

**M.Sc.****2011****4th Semester Examination****PHYSICS****PAPER—PH-2202***Full Marks : 40**Time : 2 Hours**The figures in the right-hand margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.**Illustrate the answers wherever necessary.***Group—A***(Marks : 20)*

1. Answer any five from the following : 2×5
- (a) Discuss the exchange forces between the nucleons.
  - (b) On the basis of the extreme single particle shell model, predict the spin and parity of the ground state of  ${}_9\text{F}^{17}$  and  ${}_{16}\text{G}^{31}$  nuclei.
  - (c) What do you mean by single and double magic nuclei, discuss with examples?
  - (d) Graphically discuss the compound nuclear reaction mechanism to explain nuclear reactions.
  - (e) Discuss the basic principle of the time of flight method in neutron spectroscopy.

*(Turn Over)*

- (f) State and discuss the IPM and S.I.M. with examples.
- (g) What do you understand by the level width ( $\Gamma$ ) and level separation ( $D$ ) between the levels of Continuum in nuclear reactions?
- (h) What are the sources of neutrons?

2. Answer any one bit :

10>

- (a) Write the wave equation for the ground state of the deuteron and solve it to obtain an expression connecting the depth ( $U_0$ ) and range ( $r_0$ ) of nuclear potential with the binding energy of deuteron ( $B$ ).  
2-

- (b) What are thermal neutrons? Calculate the most probable velocity and most probable energy of neutrons at room temperature ( $20^\circ\text{C}$ )

How can you establish that neutrons at low energies behave like a gas. 2+5+2-

### Group—B

(Marks : 20)

Answer Q. No. 1 and any one from the rest.

1. Answer any four of the following :

4×2

- (a) What do you mean by 'local' gauge invariance and 'global' gauge invariance?
- (b) Assuming that Wick's theorem holds for product of  $n$  fields, show that it holds also for the product of  $(n + 1)$  fields.

- (c) State and discuss Wick's expansion theorem.
- (d) Investigate whether or not  $\eta$  exists for

$$\Lambda(\partial) = \gamma\partial + m \frac{1 + \gamma\partial}{2}$$

- (e) Show that appropriate Feynman diagrams can be drawn to describe the second order S-matrix element for the Compton scattering.
- (f) Justify why a waveform interpretation of the Klein-Gordon equation is not possible.

2. (a) Show that

$$\{\psi(t, \vec{x}), \psi^\dagger(t, \vec{y})\} = \delta^3(\vec{x} - \vec{y})$$

for Dirac field.

- (b) Explain time-order product and normal order product.

- (c) If  $\hat{N} = \int d^3p a^\dagger(p)a(p)$  be the number operator in Fock space, then show that

$$[\hat{N}, a^\dagger(\mathbf{k})] = a^\dagger(\mathbf{k})$$

$$[\hat{N}, a(\mathbf{k})] = -a(\mathbf{k})$$

4+2+2+2

3. (a) Consider the Lagrangian of a real scalar field  $\phi$

$$L = \frac{1}{2}(\partial_\mu \phi)^2 - V(\phi)$$

where  $V(\phi) = \frac{1}{2}\mu^2\phi^2 + \frac{\lambda}{4}\phi^4$  with  $\lambda > 0$ .

- (i) What is the symmetry under which the above Lagrangian is invariant?
- (ii) Sketch the potential  $V(\phi)$  for  $\mu^2 < 0$  and  $\mu^2 > 0$ .
- (iii) Consider the quantum fluctuation  $\eta(x)$  about the minimum for  $\mu^2 < 0$ . How is the above Lagrangian modified under this transformation

$\phi(x) = v + \eta(x)$ ;  $v$  is the minimum for  $\mu^2 < 0$  case. What can you conclude from the new Lagrangian? Does this Lagrangian possess the above symmetry in (i)? 1+2+2

(b) For a Higg's boson multiplet  $L_\phi = (D^\mu \phi)^\dagger (D_\mu \phi) - \mu^2 \phi^\dagger \phi - \lambda(\phi^\dagger \phi)^2$

where  $D_\mu = \partial_\mu + igT_a^{(n)}W_\mu^a + ig'YB_\mu$

with  $T_a^{(n)}$  denote generators of  $SU(2)$  and  $\phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$  for charged field and neutral field.

Prove that mass of W-boson is  $\frac{1}{2}gv$  and that for

$Z^0$ -boson is  $\frac{v}{2}\sqrt{g^2 + g'^2}$ .

where  $g, g'$  are coupling constants. 2+3