

2019

B.Sc. (Honours)

4th Semester Examination

MATHEMATICS

Paper - SEC2T

Full Marks : 40

Time : 2 Hours

*The figures in the margin indicate full marks.
Candidates are required to give their answers
in their own words as far as practicable.
Illustrate the answers wherever necessary.*

1. Answer any *two* from the following : 2×2
- (a) Define isolated vertex and pendent vertex.
 - (b) Is it possible to construct a graph with 11 vertices such that 2 vertices has degree 3 and remaining vertices of degree 4? What will be the number of edges?
 - (c) Define complete and Bipartite graph with example.

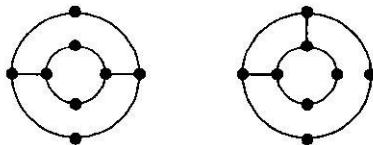
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2. Answer any *one* from the following : 5×1

- (a) Show that a simple graph with n vertices and k -components can have at most

$$\frac{(n-k)(n-k+1)}{2} \text{ edges.} \quad 5$$

- (b) (i) Define isomorphism of a graph. Are the following figures isomorphic? Justify? 1+2



- (ii) Prove that the number of edges in a bipartite graph with n vertices is at most

$$\frac{n^2}{4}. \quad 2$$

3. Answer any *two* from the followings : 5×2

- (a) Show that a given connected graph G is an Euler graph iff all vertices of G are of even degree. 5

- (b) Define Hamiltonian circuit. Show that every complete graph K_n , for all n , is a Hamiltonian

graph. Draw a connected 3-regular graph containing a bridge. 1+2+2

(c) Let adjacent matrix of a graph G is given by

$$A(G) = \begin{bmatrix} 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 \end{bmatrix}$$

Find the nature of the graph, the number of vertices and edges. Also draw the graph. 5

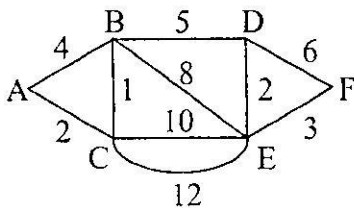
4. Answer any **two** from the followings : 2×2

- (a) Define out degree and indegree of a directed graph with example.
- (b) Find the rank and nullity of the complete graph k_n and complete bipartite graph $k_{m, n}$.
- (c) Prove that a graph has no cut vertex if every pair of vertices contained in same circuit.

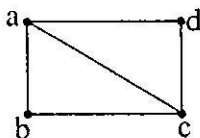
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5. Answer any *one* from the followings : 10×1

- (a) Write down Dijkstra's algorithm and find the shortest path from the vertex A to F in the following graph using this method. 10



- (b)(i) Find all possible spanning trees of the graph 4



- (ii) Prove that if an edge is added to a tree it must produce a circuit. 3
- (iii) Show that every tree with $n(\geq 2)$ vertices has at least two pendent vertices. 3
6. Answer any *one* from the followings : 5×1

- (a) Prove that a tree with n vertices has $(n-1)$ edges. 5

- (b) Define a binary tree. Show that the number of vertices n in a strictly binary tree is always odd. Find the number of pendent vertices in a strictly binary tree. 1+2+2

7. Answer any *one* from the followings : 2×1

- (a) Show that the height of a complete binary tree with n -vertices is $\lceil \log_2(nH) - 1 \rceil$.
- (b) Show that every connected graph has at least one spanning tree.

Computer Graphics

1. Answer any *five* questions : 2×5

- (a) What is pixels? Explain the frame buffer. in 600*400 pixel, how may K bytes does a frame buffer need?
- (b) What do you understand by horizontal and vertical retrace in raster system?
- (c) What do you understand by homogenous co-ordinate?

[Turn Over]

- (d) What is shearing transformation?
- (e) What do you understand by parallel projection?
- (f) Discuss the properties of the Bezier and B-Spline curves?
- (g) What are 3-D transformation?
- (h) Prove that two 2D rotation about origin; commute i.e. $R_1R_2 = R_2R_1$.

2. Answer any *four* questions : 5×4

- (a) Translate the square ABCD whose co-ordinate are $A(0, 0)$, $B(3, 0)$, $C(3, 3)$ and $D(0, 3)$ by 2 units in both directions and then scale it by 1.5 units in x -direction and 0.5 units in y -direction.
- (b) Use the Cohen-Sutherland algorithm to clip line $P_1(70, 10)$ and $P_2(100, 10)$ against a window lower left hand corner $(50, 10)$ and upper right hand corner $(80, 40)$.
- (c) Construct enough points on the Bezier curve whose control points are $P_0(4, 2)$, $P_1(8, 8)$, $P_2(16, 4)$ to draw an accurate sketch
 - (i) What is the degree of the curve?
 - (ii) What are the co-ordinates at $\mu = 0.5$?

(d) Explain the following :

(i) A-buffer

(ii) Z-buffer

(e) Write short note on :

(i) Windowing and Viewport

(ii) 3-D Clipping

(iii) 3-D geometric primitives

3. Answer any *one* question :

10×1

(a) Explain DDA line drawing algorithm with example.

(b) Write all the steps of mid point circle generating algorithm?

[Turn Over]

Operating System : Linux

1. Answer any *five* questions : 2×5
- (a) Define operating system and list the basic services provided by operating system.
 - (b) What are differences between macro kernel and micro kernel?
 - (c) Justify whether following statements are true or false
 - (i) The user application interacts directly with O.S.
 - (ii) Shell is part of operating System
 - (d) What is a boot loader?
 - (e) Explain the cut command.
 - (f) Write a note on the contents of the etc/passwd file.
 - (g) What are the duties of a system administrator?
 - (h) What is meant by Linux disk management?

2. Answer any *four* questions : 5×4
- (a) Explain the following commands with examples :
ls, rm, cp, mv, chown, chmod.
 - (b) Which are the different file systems supported by Linux? Which feature of Linux makes this support possible (Virtual File Systems Layer)?
 - (c) Describe the following commands: chown, chmod, expr.
 - (d) Explain the purpose of the following files : /etc/hosts.conf, /etc/hosts, /etc/resolv.conf
 - (e) Write a note on telnet, ftp, rsync, and rsh. Why are these services called insecure services?
 - (f) Write short notes on : (a) message passing
(b) shell
3. Answer any *one* question : 10×1
- (a) (i) What are the design principles of Linux operating systems? Explain.
 - (ii) Explain the process management model of linux operating system.

[Turn Over]

(b) Write short notes on (any two) : 5×2

- (i) Process states
 - (ii) Critical section
 - (iii) Race condition
 - (iv) Starvation
 - (v) Linux Security
 - (vi) Ext3 file system
 - (vii) Pipes
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