

2019

B.Sc.

2nd Semester Examination

COMPUTER SCIENCE (Honours)

Paper - C4T

(Discrete Structure)

Full Marks : 60

Time : 3 Hours

*The figures in the margin indicate full marks.  
Candidates are required to give their answers  
in their own words as far as practicable.*

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|--|------|
| 1. Answer any ten questions.                     | 10×2 |
| (a) Define master theorem.                       | 2    |
| (b) Define Planar Graphs.                        | 2    |
| (c) Define De Morgan's law.                      | 2    |
| (d) Write, principle of inclusion and exclusion. | 2    |
| (e) Prove that $3n^2 + 2n + 5 = O(n^2)$ .        | 2    |

*[ Turn Over ]*

- (f) Define  $\Omega$  (Big-omega) notation in complexity. 2
- (g) Define generating function. 2
- (h) Write down basic characteristics of an Algorithm.
- (i) Define cut set and cut vertex. 2
- (j) Define Euler graph. 2
- (k) Give an example of a relation which is Reflexive and Transitive but not symmetric. 2
- (l) Define Adjacency matrix of a graph. 2
- (m) Define symmetric difference between two sets with an example. 2
- (n) Prove that number of odd degree vertices in a graph is always even. 2
- (o) Define Bijective mapping with an example. 2
2. Answer any *four* questions. 4×5
- (a) Define Tautology and Contradiction. Using Truth table prove that,
- $$(p \rightarrow q) \wedge (r \rightarrow q) \equiv (p \vee r) \rightarrow q \quad 2+3$$

(b) Using Mathematical induction prove that :

$$2^n < \underline{n} \text{ for } n \geq 4. \quad 5$$

(c) For any three arbitrary sets A, B, C, prove that

$$(i) A - (B \cup C) = (A - B) \cap (A - C)$$

$$(ii) (A \cap B) \cap (A - B) = \phi \quad 2\frac{1}{2} + 2\frac{1}{2}$$

(d) If  $R$  be a relation in the set of integers  $Z$  defined by

$$R = \{(x, y) : x \in z, y \in z, \\ (x - y) \text{ is divisible by } 6\}$$

Prove that  $R$  is an equivalence relation. 5

(e) Solve the following recurrence relation.

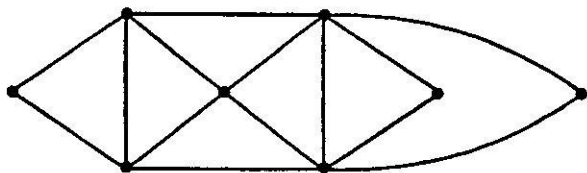
$$a_r - 3a_{r-1} + 3a_{r-2} - a_{r-3} = 0 \quad 5$$

given that,  $a_0 = 2, a_1 = 1, a_2 = 1.$

[ Turn Over ]

(f) Colour the following graph :

5

Answer any *two* questions :

2×10

3. (a) Prove that in a simple graph with  $n$  vertices and  $K$  components can not have more than  $(n-k)(n-k+1)/2$  edges. Prove that  $E = I + 2n$ , where  $E$  is the external path length,  $I$  is the internal path length and  $n$  is the nodes having two children. 7+3

- (b) (i) Find asymptotic relation for the recurrence relation using Master theorem

$$T(n) = 2T(n/2) + n^2$$

- (ii) Find the asymptotic using substitution method :

$$T(n) = 6T(n/3) + 2n - 1,$$

$$T(n) = 2 \text{ for } n = 1$$

5+5

- (c) (i) Prove that a tree with  $n$  vertices contains  $(n - 1)$  edges.
- (ii) Define graph isomorphism with an example.
- (iii) Prove that a connected graph contains an Eulerian trail, but not an Eulerian circuit, if and only if it has exactly two vertices of odd degree. 5+2+3
- (d) (i) Solve the recurrence relation using generating function :

$$a_r - 5a_{r-1} + 6a_{r-2} = 2^r + r ; a_0 = 1, a_1 = 1$$

- (ii) 900 students appeared for two papers in Mathematics. 740 students passed in paper-I and 650 students in paper-II. If 625 students passed in both, find the number of students who failed in both.
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