

2019

B.Sc.

2nd Semester Examination  
**ECONOMICS (Honours)**

Paper - C4T

(Mathematical Methods in Economics - I)

Full Marks : 60

Time : 3 Hours

*The figures in the margin indicate full marks.  
Candidates are required to give their answers  
in their own words as far as practicable.*

**Group - A**

Answer any *ten* questions.

10×2

1. (a) What do you mean by eigen values ?
- (b) What are quasi convex functions ?
- (c) Define feasible solution in LPP.
- (d) What are implicit functions ?
- (e) What is convex set ?

[ Turn Over ]

- (f) What do you mean by point of inflexion ?
- (g) Set up a non-linear programming problem.
- (h) Write the Kuhn-Tucker conditions for minimization problem.
- (i) Distinguish between endogenous and exogenous variables.
- (j) What do you mean by inverse of a square matrix ?
- (k) What are parameters ?
- (l) Given the demand function  $p = \frac{36}{q-36} + 12$  find the maximum revenue.
- (m) Find the determinant of the matrix :

$$\begin{bmatrix} 2 & 4 \\ 3 & 1 \end{bmatrix}$$

- (n) Prove that the elasticity of substitution for a Cobb-Douglas production function is unity.
- (o) If the demand function for a profit maximizing monopolist is  $P = 274 - Q^2$  and  $MC = 4+3Q$ , find consumer surplus.

( 3 )

**Group - B**

Answer any *four* questions.

4×5

2. Consider the following linear programming problem (LPP) :

$$\text{Maximize Profit } (\pi) = 2x_1 + 5x_2$$

$$\text{Subject to } x_1 + 4x_2 \leq 24$$

$$3x_1 + x_2 \leq 21$$

$$x_1 + x_2 \leq 9$$

$$x_1 \geq 0, x_2 \geq 0$$

Construct the dual problem.

3. Suppose  $u = x_1^{\alpha_1} x_2^{\alpha_2}$  is a utility function. If  $x_1 p_1 + x_2 p_2 = M$  is the budget constraint, then find the demand function for  $x_1$ .
4. Set up a complete Keynesian model with three markets — labour market, commodity market and money market.

[ Turn Over ]

5. Solve the following LPP :

$$\text{Max } \pi = 25x_1 + 50x_2$$

$$\text{Subject to } 9x_1 + 12x_2 \leq 144$$

$$10x_1 + 6x_2 \leq 120$$

$$x_2 \leq 9$$

$$x_1 \geq 0, x_2 \geq 0$$

6. Consider the simple utility maximization problem subject to a budget constraint in a 2 good case. Interpret the Lagrangian multiplier used in the maximization exercise.
7. What do you mean by minimum value function ?

### Group - C

Answer any *two* questions. 2×10

8. Write a note on Duality theorem in linear programming.
9. Find the own price elasticity, the crossprice elasticity and the income elasticity for the following demand function at point

$$(p_1, p_2, y) = (2, 4, 120), Q_1 = 20 - 9p_1 - \frac{1}{2}p_2$$

$$+ \frac{1}{2}p_1 p_2 + \frac{1}{6}y$$

Also identify whether Good 1 and 2 are complements or substitutes.

10. Assume that a monopolist faces the following linear demand and cost curves :

$$p_1 = 80 - 5q_1, p_2 = 180 - 20q_2 \text{ and}$$

$$C = 50 + 20 (q_1 + q_2)$$

- (i) What will be her profit maximizing level of sales in each market ? Also calculate her profit.
- (ii) Show that if the monopolist could not segregate the two markets and were forced to treat them as one, her profits would have been lower.

6+4

11. Distinguish between slack and surplus variables. How are they used in LPP ?

5+5

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